



Work in progress

Thomas Zwinger



CSC – Suomalainen tutkimuksen, koulutuksen, kulttuurin ja julkishallinnon ICT-osaamiskeskus

Current developments



A simple permafrost model

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A numerical investigation of ice-lobe–permafrost interaction around the southern Laurentide ice sheet

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A simple permafrost model

- Single heat transfer equation for mixtures:
$$\frac{\partial}{\partial z} \left(K \frac{\partial T}{\partial z} \right) = C \frac{\partial T}{\partial t}$$
- Apparent volumetric heat capacity:
$$C = C_v + L \frac{\partial \theta_u}{\partial T}$$
- Volumetric water content:
$$\theta_u = \begin{cases} (\rho_b / \rho_u) a T_*^b & (T < T_{\text{pmp}} - \Delta T) \\ \theta_t & (T \geq T_{\text{pmp}} - \Delta T) \end{cases}$$
- Effective conductivity by weighted geometric mean:
$$K = K_b^{\theta_b} K_u^{\theta_u} K_i^{\theta_i}$$

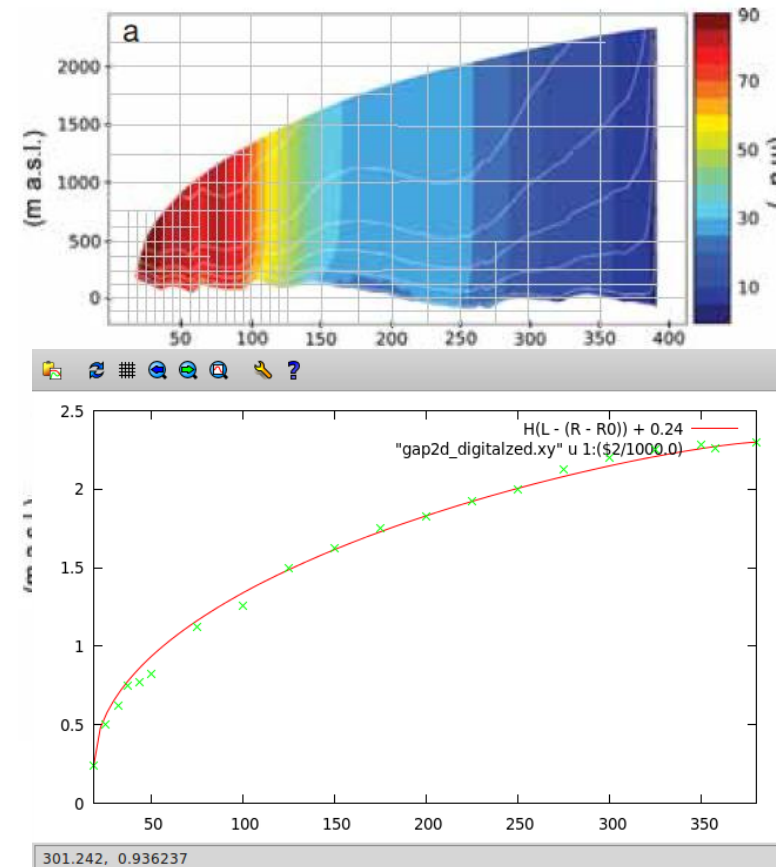
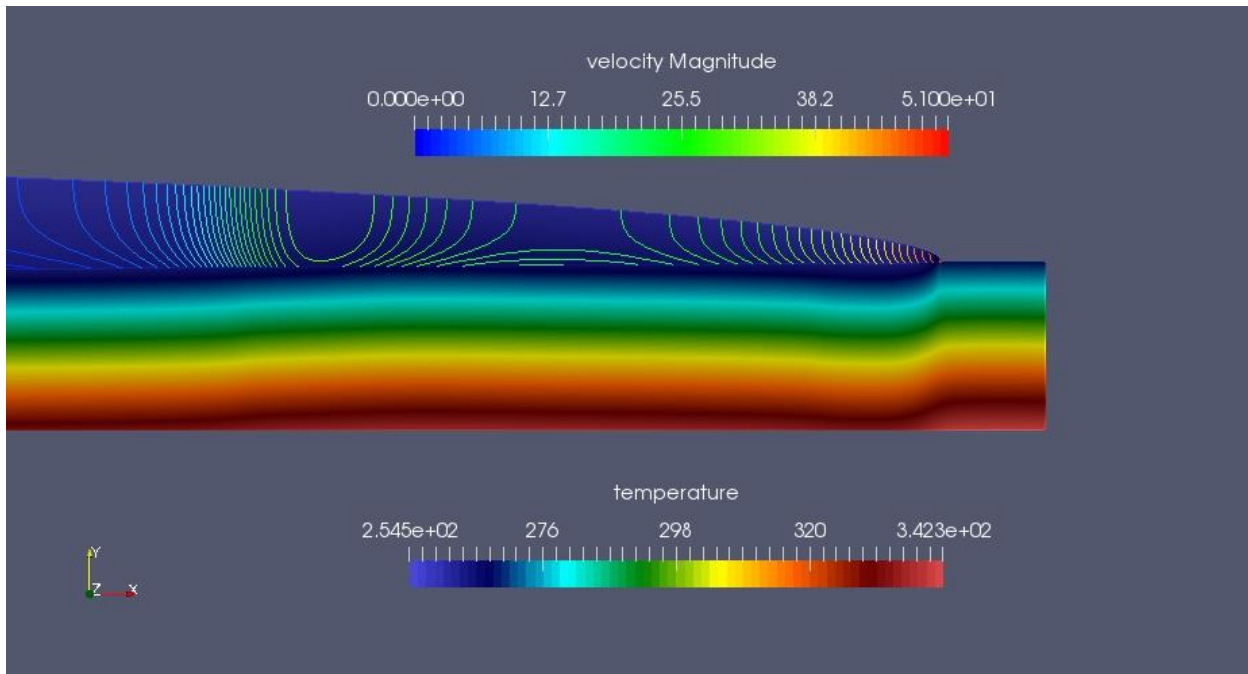
bedrock

water

ice
- Effective volumetric heat capacity:
$$C_v = \theta_i C_i + \theta_u C_u + \theta_b C_b \quad \theta_b = 1 - \theta_t, \quad \theta_t = \theta_u + \theta_i.$$

A simple permafrost model

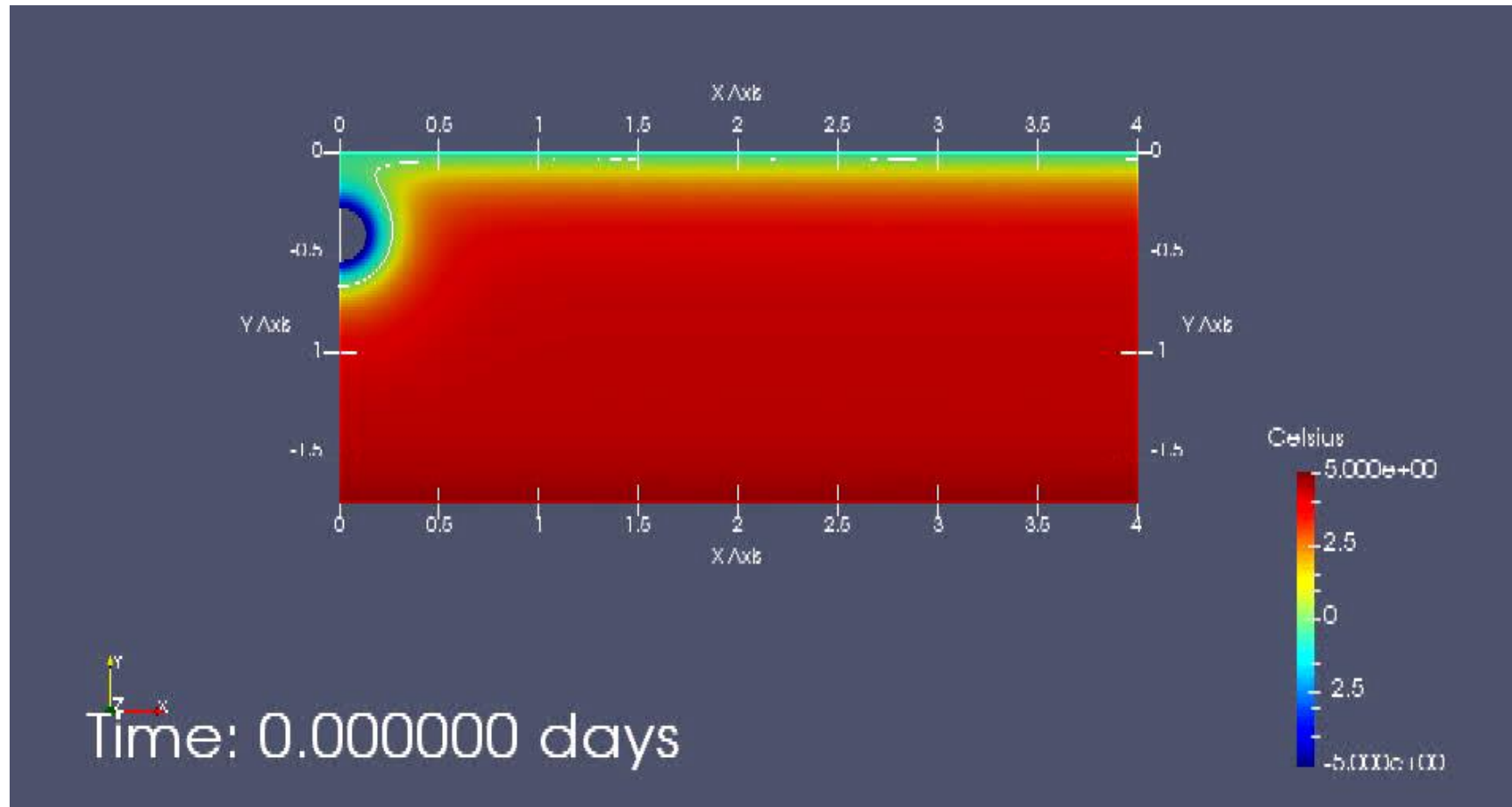
- GAP test-site: Brinkerhoff et al., 2015
- Looks almost like a Bueler profile
- Based on steady state assumption



A simpler permafrost model

- Separate branch on GitHub: [ElmerCSC/elmerfem/permafrost](https://github.com/ElmerCSC/elmerfem/permafrost)
- Cooperation between CSC, Denis Cohen and Juha Hartikainen
- Currently following new aspects available there:
 - Multi-level internal extrusion
 - Structured Mesh functionality for two layers (in elmerice and devel branch)
 - Simple model from Cutler et al. 2000 implemented using single HeatSolver with special switches for material parameters
- Development of coupled permafrost model:
 - Heat conduction and convection (done)
 - Water transport (Darcy)
 - Salinity transport
 - Porosity evolution

Heat transfer in soil around sub-zero gas-pipe



Glacial Isostatic Adjustment

- Working on coupled elastic/viscous model (L. Jong, UTAS)
 - Based on P. Wu, 2004 paper
 - Using PREM data
- Currently LLRA model (too embarrassingly simple to push to repository)



New rheology model

- Cooperation with UTAS (Jong, LeGallais, Treverrow, Warner)
 - Testing new rheology against laboratory experiments
- Scalar rheology using enhancement factor (Budd et al. 2013)
 - Co-linear model
 - Referred to as “ESTAR” rheology
- Finding the non-rotating shear plane
 - In principle this is a tensor-algebraic exercise
 - Plan to implement in near future into Elmer/Ice