

Gas Tungsten Arc Welding heat transfer simulation

1. The GTAW Heat transfer problem:

The GTA Welding or TIG (Tungsten Inert Gas) process is studied in a simple case involving only the Heat transfer physics. This document describes the coefficients used in the state equation and its boundary conditions in order to understand the gtaw.sif attached to the post (as well as the mesh files...). This is just a preliminary work. I hope to add the Navier-Stokes, the electromagnetism equations in order to take into account the Lorentz force and the free surface deformation on the weld-pool surface. Figure 1, here below, depicts all the phenomena involved in GTA Welding.

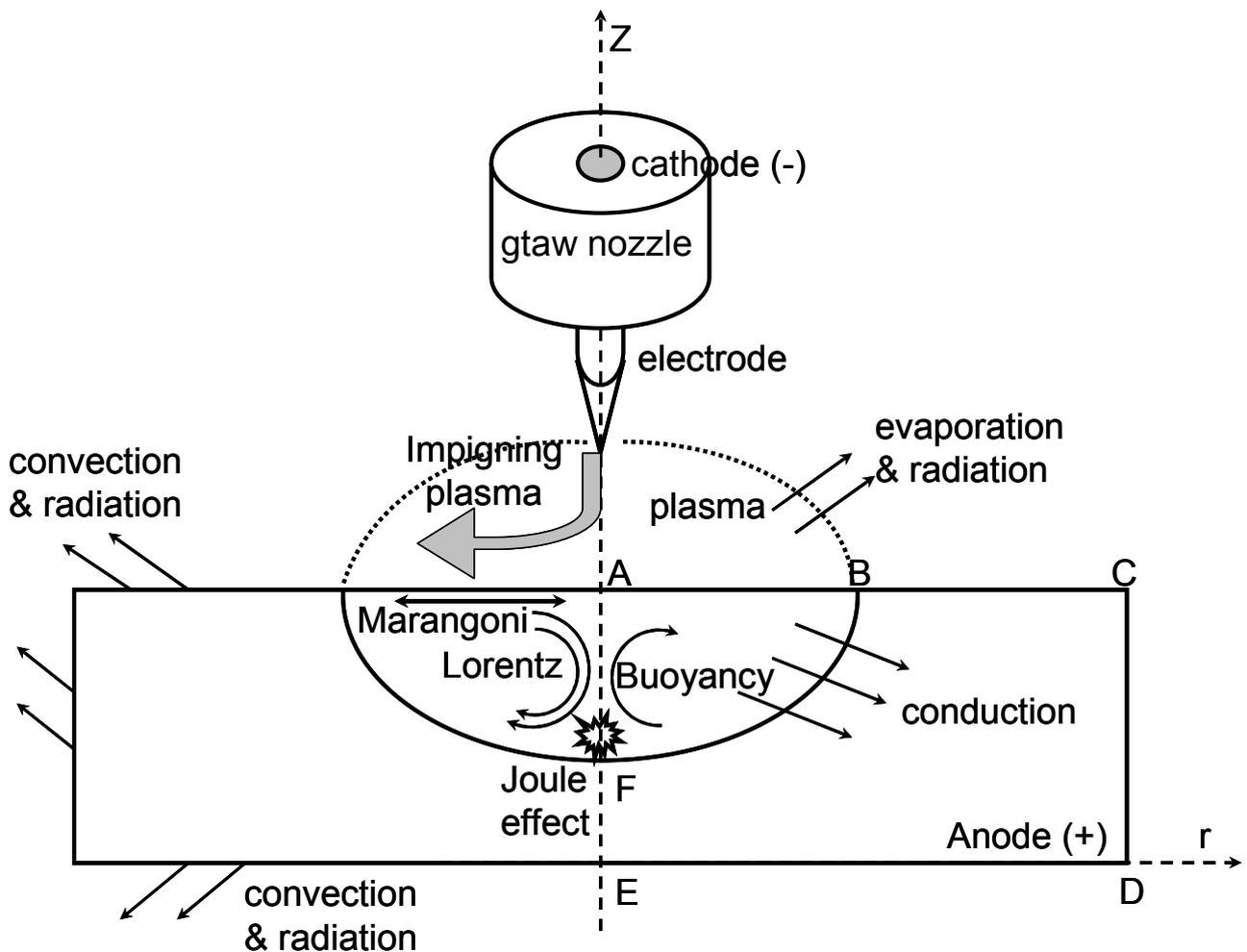


Figure 1: magneto-hydrodynamic problem involved in GTAW.

$$\rho C_p^{eq} \frac{\partial T}{\partial t} - \frac{1}{r} \frac{\partial}{\partial r} \left(r \lambda \frac{\partial T}{\partial r} \right) - \frac{\partial}{\partial z} \left(\lambda \frac{\partial T}{\partial z} \right) = 0$$

With T is the temperature field. ρ , C_p and λ are respectively the mass density, specific heat and thermal conductivity of the Stainless Steel Metal.

The heat transfer boundary conditions are (it refers to figure 2):

$$\rightarrow \text{On the top surface } \Gamma_1 \cup \Gamma_2 : -\lambda \frac{\partial T}{\partial z} = -\Phi(r, t) + h(T - T_0) + \varepsilon \sigma (T^4 - T_0^4)$$

$$\rightarrow \text{On the lateral side } \Gamma_3 : -\lambda \frac{\partial T}{\partial r} = h(T - T_0) + \varepsilon \sigma (T^4 - T_0^4)$$

$$\rightarrow \text{On the bottom surface } \Gamma_4 : \lambda \frac{\partial T}{\partial z} = h(T - T_0) + \varepsilon \sigma (T^4 - T_0^4)$$

$$\rightarrow \text{On the symmetry axis : } -\lambda \frac{\partial T}{\partial r} = 0$$

$$\rightarrow \text{The initial condition is: } T(r, t = 0) = T_0$$

$\Phi(r)$ is a surface heat flux exchanged between the plasma arc and the work-piece. We will assume that this heat flux distribution obey to a Gaussian distribution. So it can be written as follows:

$$\Phi(r, t) = \eta \frac{1}{2} \frac{U_s \cdot I_s}{\pi r_b^2} e^{-\frac{1}{2} \left(\frac{r}{r_b} \right)^2} \text{ where } U_s \text{ is the welding tension, } I_s \text{ is the welding intensity, } \eta \text{ is the}$$

GTAW efficiency and r_b is called the Gaussian radius.